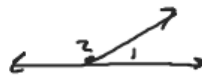


**Spiral Review**



1. Find a counter example to show that the statement is not true. If angles are supplementary then they form a linear pair.



2. Find the coordinates of the point  $\frac{7}{10}$  of the way from A to B.

Distance x-values  
 $9 - (-4) = 13$

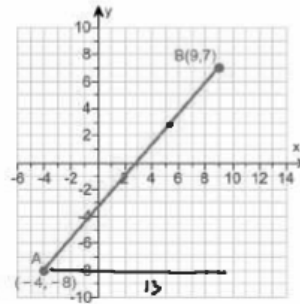
$(13)\left(\frac{7}{10}\right) = \frac{91}{10} = 9.1$

Distance y-values  
 $7 - (-8) = 15$

$15\left(\frac{7}{10}\right) = 10.5$

$-4 + 9.1 = 5.1$        $(5.1, 2.5)$

$-8 + 10.5 = 2.5$



3. Consider the statement: If James has 2 dimes, then he has at least 20 cents.  
a. Is this a true statement? Justify your reasoning.

True

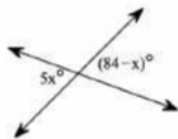
b. Write the converse of the given statement. Is the converse a true statement?

Explain.

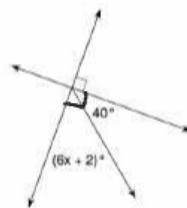
If James has at least 20 cents, then he has at least 2 dimes.

False      20 pennies  
                 5 Nickels

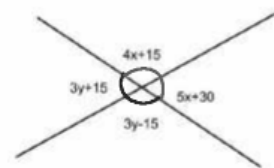
4. Find the value of the variable.



$5x = 84 - x$   
 $6x = 84$   
 $x = 14$



$6x + 2 + 40 = 90$   
 $6x + 42 = 90$   
 $6x = 48$   
 $x = 8$



$3y + 15 + 3y - 15 = 180$   
 $6y = 180$   
 $y = 30$   
 $4x + 15 + 5x + 30 = 180$   
 $9x + 45 = 180$   
 $9x = 135$   
 $x = 15$

**Properties of Parallel Lines**

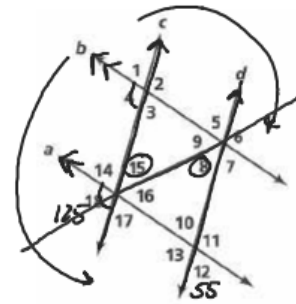
**Section: Properties of Parallel Lines**

Use the figure to answer each question in this section.

5. If  $c \parallel d, a \parallel b$ , and  $m\angle 12 = 55^\circ$ , then  $m\angle 4 = \underline{125^\circ}$

6. If  $\angle 15 \cong \angle 8$  then which two lines are parallel? Explain your answer.

*c* || *d* Converse of Alternate Int  $\angle$ 's.



$180 - 55$

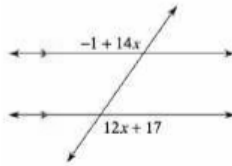
7. Find the value of  $x$ .

$-1 + 14x = 12x + 17$

$-1 + 2x = 17$

$2x = 18$

$x = 9$



8. Use the figure to the right. Lines  $r, s, t, u$  intersect as shown.

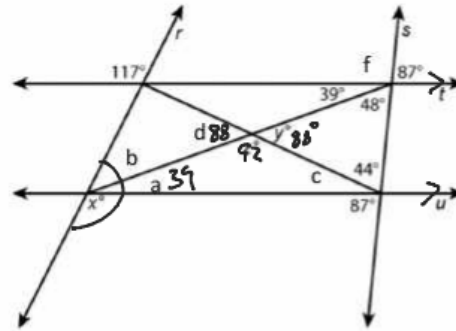
a. Which pairs of lines are parallel?

$t \parallel u$

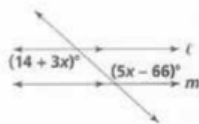
b. Find the values of the variables.

$a = \underline{39^\circ}$   $b = \underline{24}$   $c = \underline{49}$   $d = \underline{88}$

$f = \underline{93}$   $x = \underline{117}$   $y = \underline{88}$   $z = \underline{92}$



9. Find the value of the variable that will make the lines parallel.

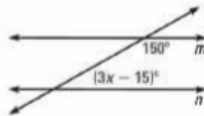


$14 + 3x = 5x - 66$

$14 = 2x - 66$

$80 = 2x$

$x = 40$

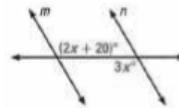


$3x - 15 + 150 = 180$

$3x + 135 = 180$

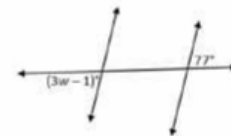
$3x = 45$

$x = 15$



$2x + 20 = 3x$

$x = 20$



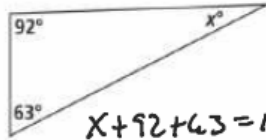
$3w - 1 = 77$

$3w = 78$

$w = 26$

**Section: Parallel Lines and the Triangle Sum – Theorem**

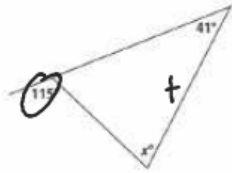
10. Find the value of the variable.



$$x + 92 + 63 = 180$$

$$x + 155 = 180$$

$$x = 25$$



$$x + 41 = 115$$

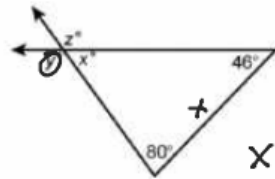
$$x = 74$$

11. Given the figure, find the value of the variables.

$$y = 46 + 80$$

$$y = 126$$

$$z = 126$$



$$x + 46 + 80 = 180$$

$$x + 126 = 180$$

$$x = 54$$

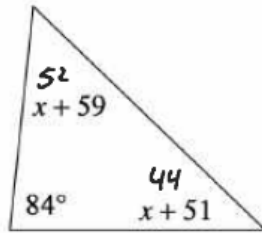
12. Find the value of x.

$$x + 59 + 84 + x + 51 = 180$$

$$2x + 194 = 180$$

$$2x = -14$$

$$x = -7$$



**Section: Slopes of Parallel and Perpendicular Lines.**

13. Are the lines, parallel, perpendicular, or neither?

Same slope      Opposite Reciprocal

Perpendicular

$$y = \frac{2}{3}x + 5$$

$$3x + 2y = 8 \rightarrow y = mx + b$$

$$\frac{2y}{2} = -\frac{3x}{2} + \frac{8}{2} \quad y = -\frac{3}{2}x + 4$$

$$\left(\frac{2}{3}\right)\left(-\frac{3}{2}\right) = -\frac{6}{6} = -1$$

14. Write an equation (slope-intercept form) for the line that is parallel to  $y = -4x + 5$  that contains the point  $(1, -6)$

$$m = -4$$

$$m = -4$$

$$y - y_1 = m(x - x_1)$$

$$y - (-6) = -4(x - 1)$$

$$y + 6 = -4x + 4$$

$$y = -4x - 2$$

$$y - y_1 = m(x - x_1)$$

15. Write an equation (slope-intercept form) for the line that is perpendicular to  $y = 3x - 2$  and passes through the point  $(9, -2)$

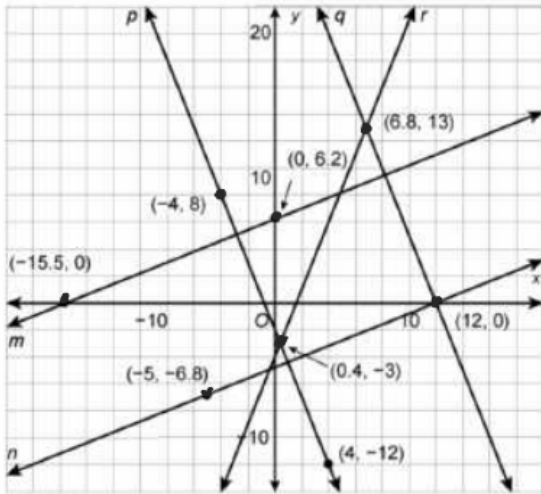
$$m = -\frac{1}{3}$$

$$y - (-2) = -\frac{1}{3}(x - 9)$$

$$y + 2 = -\frac{1}{3}x + 3$$

$$y = -\frac{1}{3}x + 1$$

16. Given the following figure, find which lines will be parallel and perpendicular. Verify using slopes.



$$\text{Slope} = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{6.2 - 0}{0 - (-15.5)} = \frac{2}{5}$$

$m \parallel n$      $p \parallel q$

$m \perp p$

$n \perp p$

$m \perp q$

$n \perp q$

$$n = \frac{0 - (-6.8)}{12 - (-5)} = \frac{6.8}{17} = \frac{2}{5}$$

$$p = \frac{-3 - 8}{.4 - (-4)} = -2.5 = -\frac{5}{2}$$

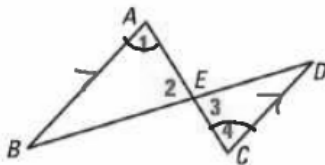
$$q = \frac{0 - 13}{12 - 4.8} = -2.5 = -\frac{5}{2}$$

$$r = \frac{13 - (-3)}{6.8 - .4} = 2.5 = \frac{5}{2}$$

### Section: Proofs

**GIVEN**  $\angle 1 \cong \angle 2, \angle 3 \cong \angle 4$

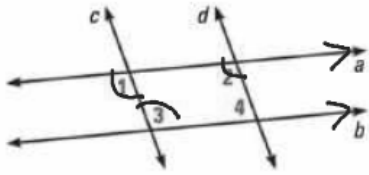
**PROVE**  $\overline{AB} \parallel \overline{CD}$



| Statement                                             | Reason                          |
|-------------------------------------------------------|---------------------------------|
| 1. $\angle 1 \cong \angle 2, \angle 3 \cong \angle 4$ | 1. Given                        |
| 2. $\angle 2 \cong \angle 3$                          | 2. Vertical $\angle$ 's         |
| 3. $\angle 1 \cong \angle 4$                          | 3. Substitution prop            |
| 4. $\overline{AB} \parallel \overline{CD}$            | 4. Converse Alt Int $\angle$ 's |

**GIVEN**  $a \parallel b$ ,  $\angle 2 \cong \angle 3$

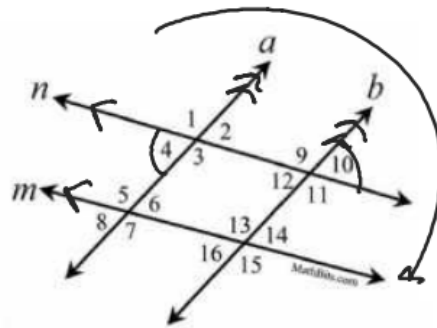
**PROVE**  $c \parallel d$



| Statement                                      | Reason                                |
|------------------------------------------------|---------------------------------------|
| 1. $a \parallel b$ , $\angle 2 \cong \angle 3$ | 1. Given                              |
| 2. $\angle 1 \cong \angle 3$                   | 2. Alt Ext $\angle$ 's $\cong$        |
| 3. $\angle 1 \cong \angle 2$                   | 3. Substitution Property              |
| 4. $c \parallel d$                             | 4. Converse Corresponding $\angle$ 's |

Given:  $m \parallel n$  and  $a \parallel b$

Prove  $\angle 4$  is supplementary  $\angle 15$



| Statement                                        | Reason                                |
|--------------------------------------------------|---------------------------------------|
| 1. $m \parallel n$ and $a \parallel b$           | 1. Given                              |
| 2. $\angle 4 \cong \angle 10$                    | 2. Alt Ext $\angle$ 's                |
| 3. $\angle 10$ and $\angle 15$ are supplementary | 3. Same-side Ext $\angle$ 's          |
| 4. $m\angle 10 + m\angle 15 = 180$               | 4. Definition of Supplementary Angles |
| 5. $m\angle 4 = m\angle 10$                      | 5. Def $\cong \angle$ 's              |
| 6. $m\angle 4 + m\angle 15 = 180$                | 6. Substitution Property              |
| 7. $\angle 4 + \angle 15$ are supp               | 7. Def of Supp $\angle$ 's            |